

WP 3000

Doppler Stack Processing

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- **The multilook processing is used:**

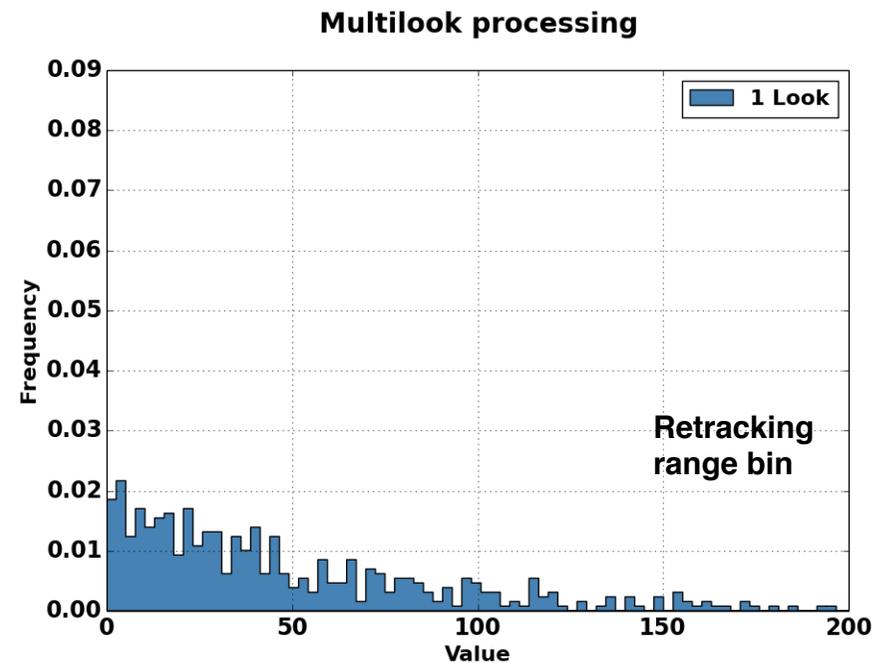
- To reduce the speckle noise
- To obtain data compression

- **Single-look**

- Probability distribution function has a exponential distribution

$$f(x, \lambda) = \lambda e^{-\lambda x}$$

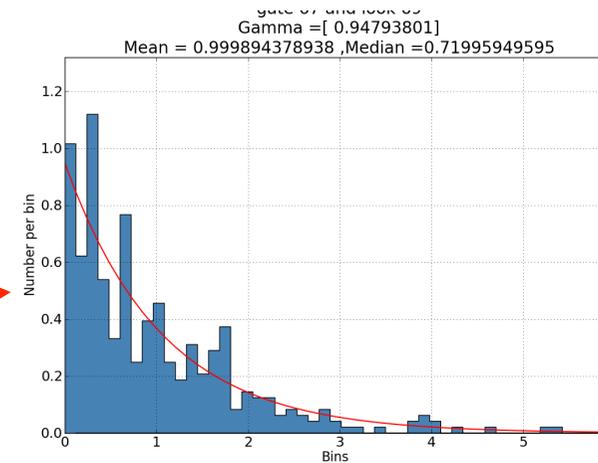
- Average value of the speckle amplitude = standard deviation



- Speckle noise law has been characterized with SIRAL data (from CPP) showing expected exponential distribution

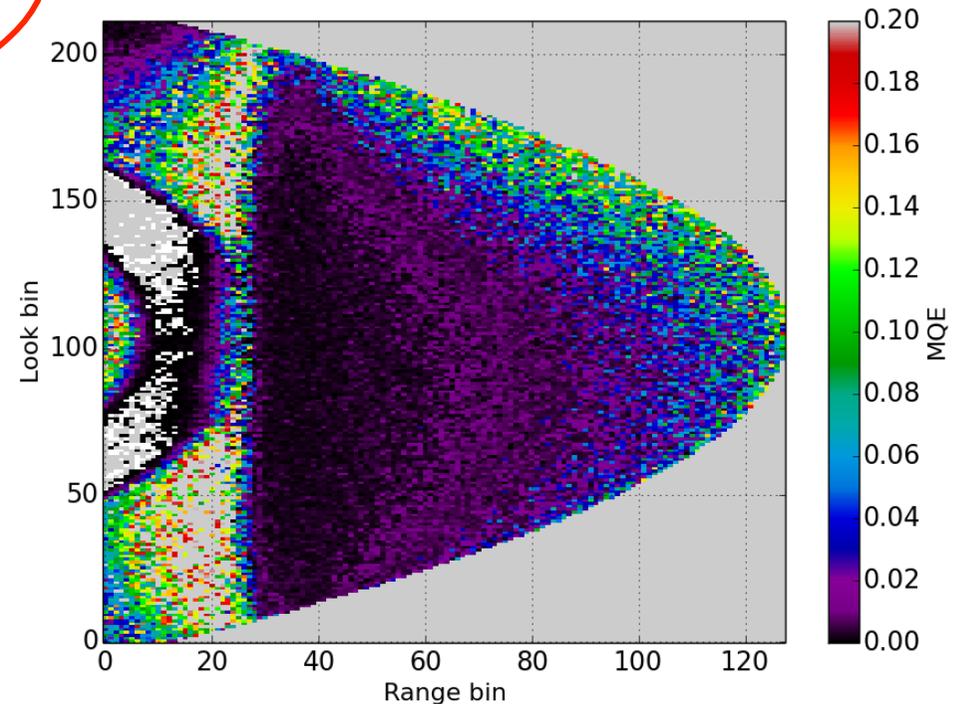
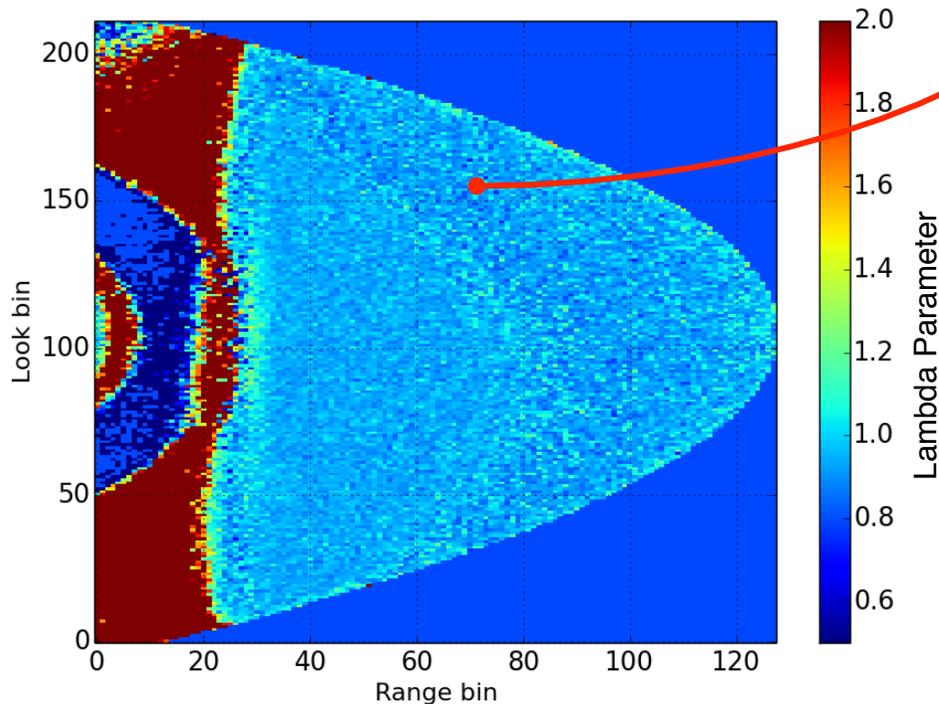
$$f(x, \lambda) = \lambda e^{-\lambda x} \quad \text{with } \lambda=1$$

- ➔ Same speckle characteristics after Doppler processing as for individual conventional altimetry pulses



Lambda Parameter for 500 stacks

Mean quadratic Error for 500 stacks



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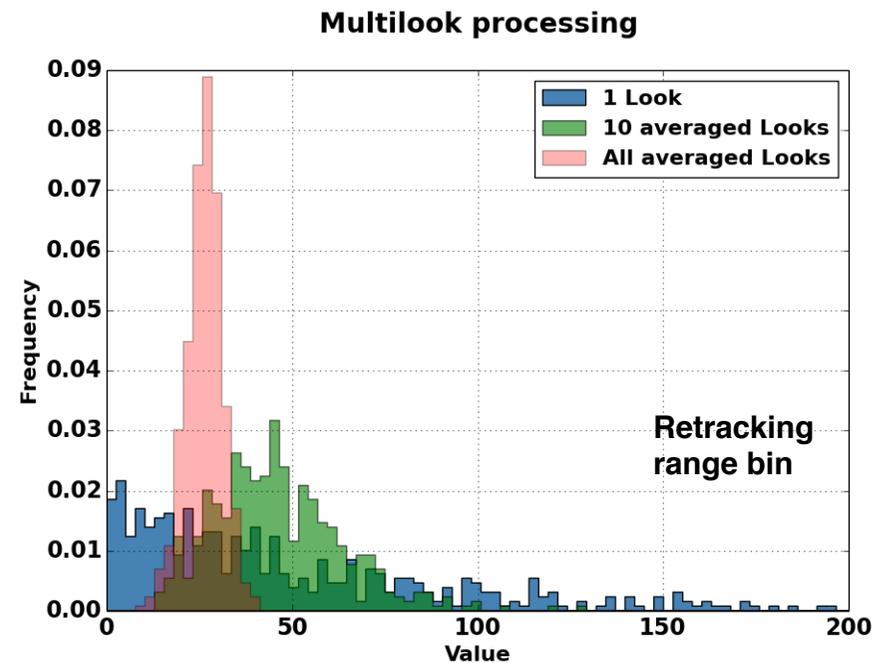
- Average value of the speckle amplitude = standard deviation

- **Multilooking**

- Incoherent addition of independent looks of the same scene
- For N-looks, the speckle amplitude has a gamma distribution

$$f(x, N; \lambda) = \frac{\lambda^N}{\Gamma(N)} e^{-\lambda x} x^{N-1}$$

- If N-looks have same intensity and shape: **Average value/standard deviation = \sqrt{N}**



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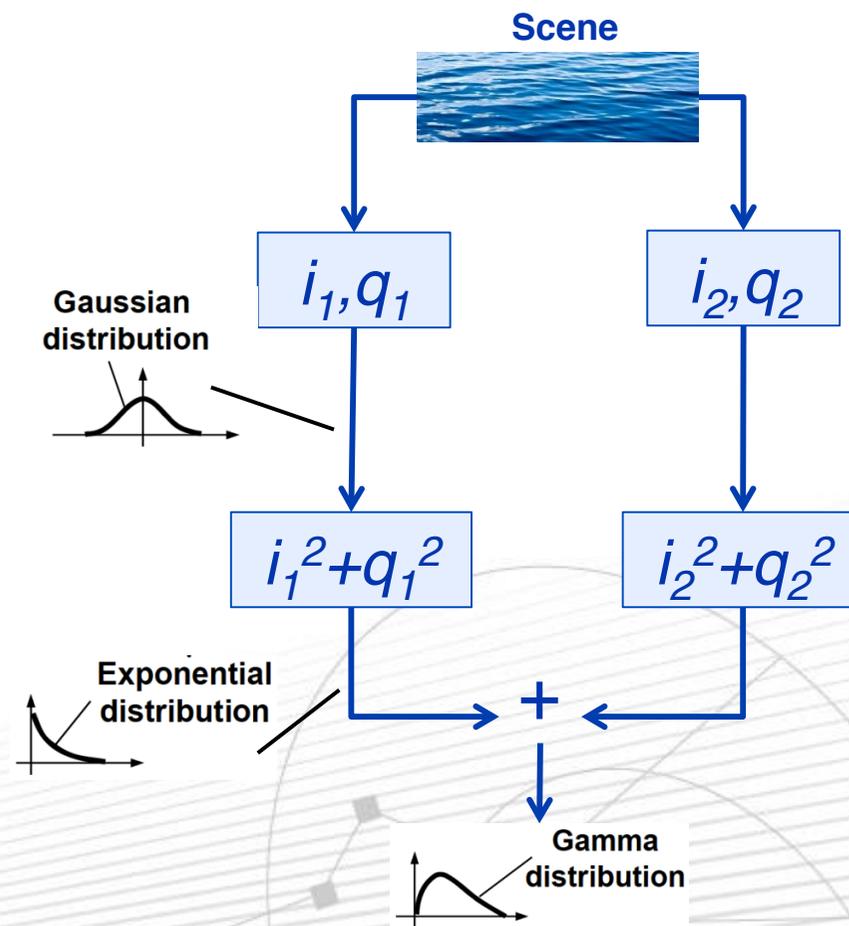
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- **Multilooking**

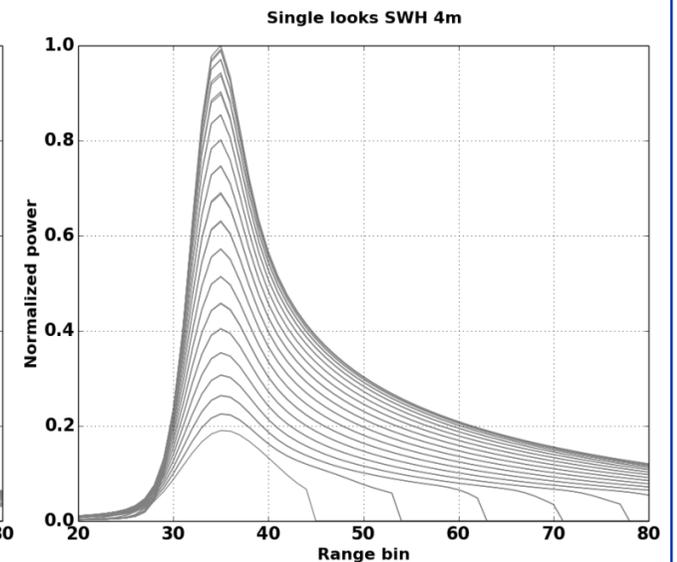
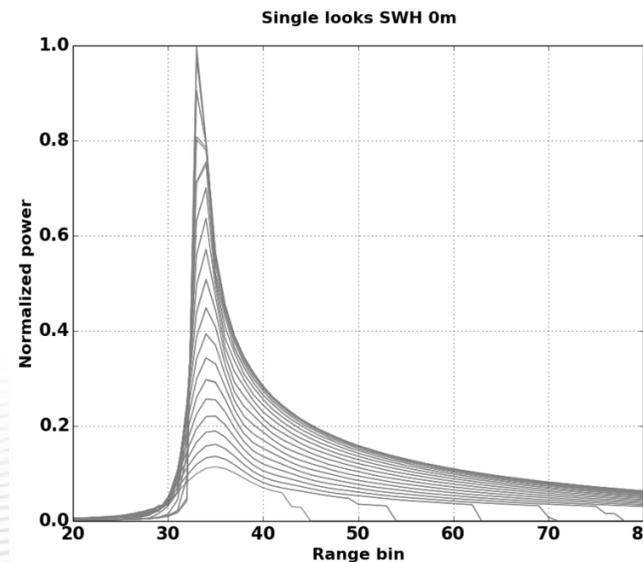
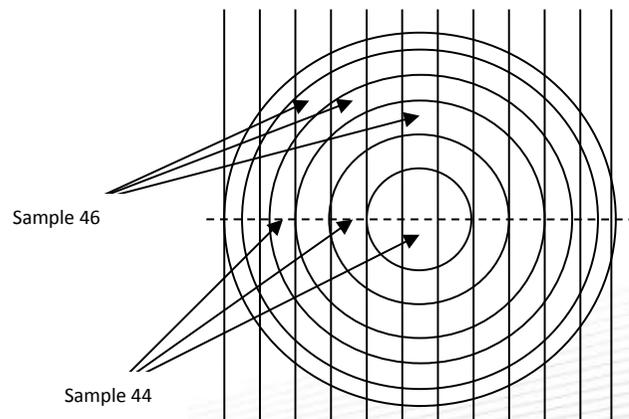
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- **But the reduction of the noise level is not as high as expected (and lower than \sqrt{N})** [*Amarouche, meeting SAR, NOC, 2013*]
 - High inhomogeneity between Doppler bins (stack)
 - Along-track variation of the mean power waveforms from look to look due to antenna gain
 - Different mean shapes in range due to inaccurate migration corrections



- **Equivalent (or effective) Number of Looks (ENL)**

- Indicates the degree of averaging in the multilook echo
- Good indicator of the speckle noise level

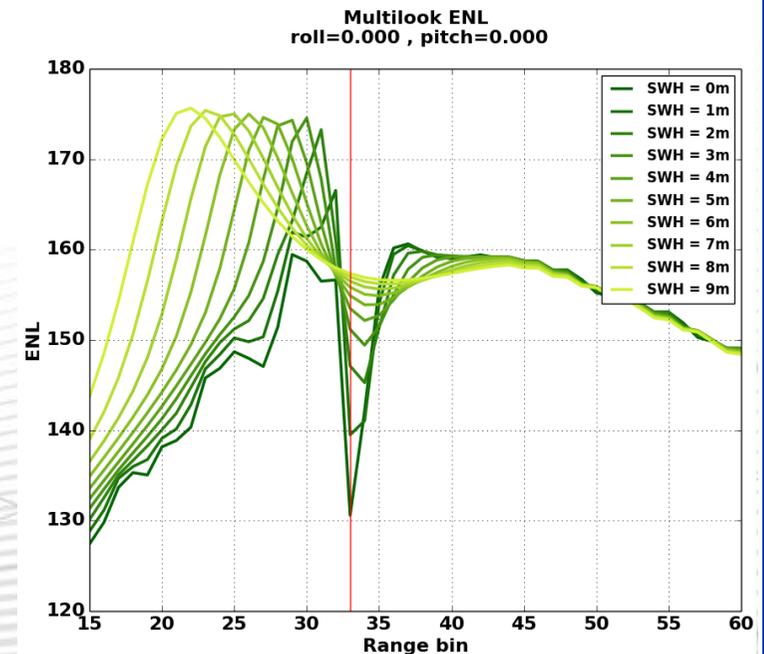
$$ENL = \left(\frac{a}{\sqrt{v}} \right)^2 = \frac{N}{1 + \frac{1}{N} \sum_{i=1}^N \left(\frac{\alpha_i}{a} \right)^2} = k \cdot N$$

Number of looks

mean power variations within stacked beams

- High speckle reduction for samples whose look-to-look discrepancies are low
- Low speckle reduction for large variation of echo amplitude
- Lowest values in the leading edge for low swh
 → increased noise level while retracking Doppler echoes at low wave height

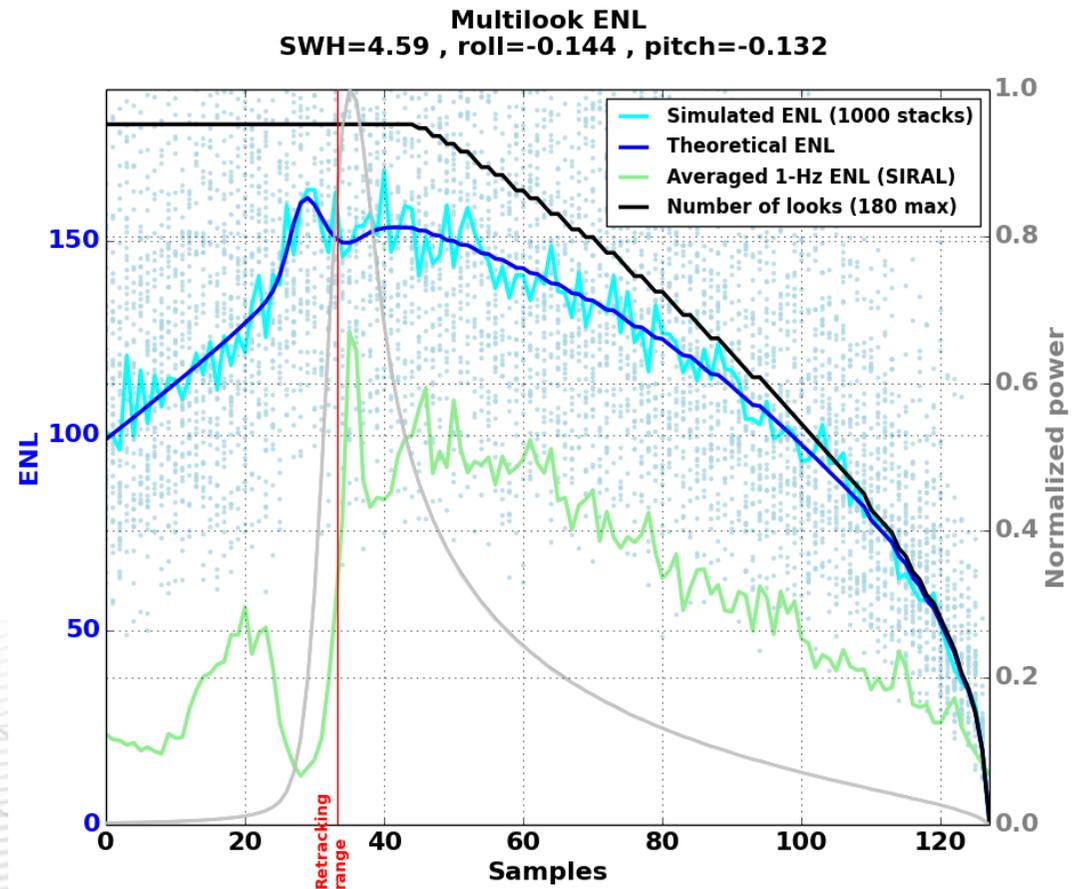
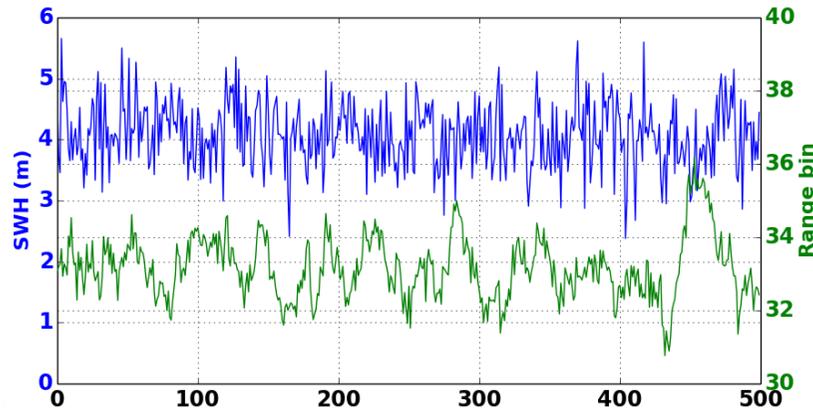
ENL for multilook echoes is lower than N and varies in range bins



- **ENL** computed with **real data** (over 500 consecutive 20-Hz data) is **even lower**

mostly due to the difficulty to gather data of homogeneous sea state and similar orbit parameters

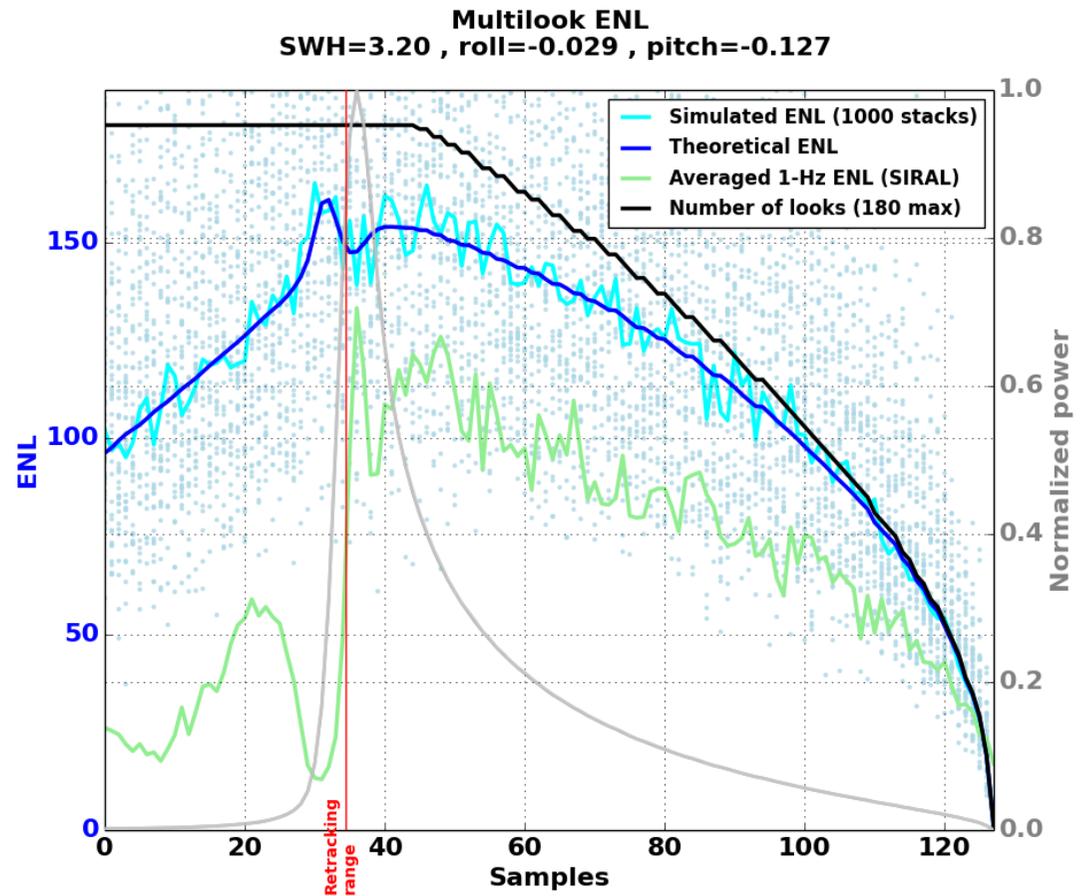
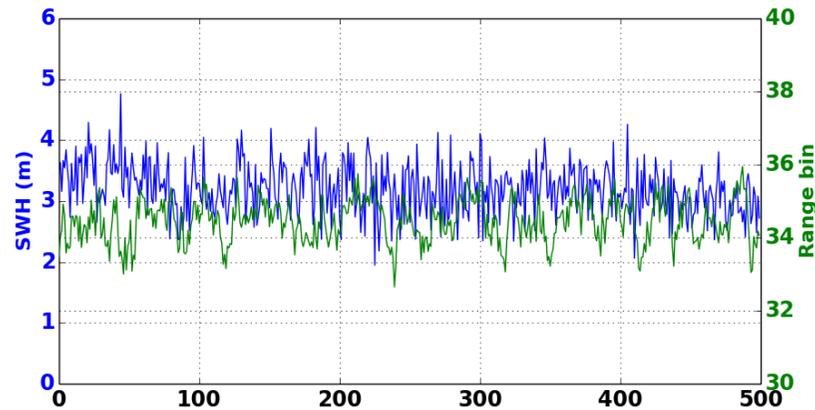
In the Agulhas SAR-mode area



- **ENL** computed with **real data** (over 500 consecutive 20-Hz data) is **even lower**

A better homogeneity in sea state and orbit parameters improve the computed ENL

In the Pacific SAR-mode area

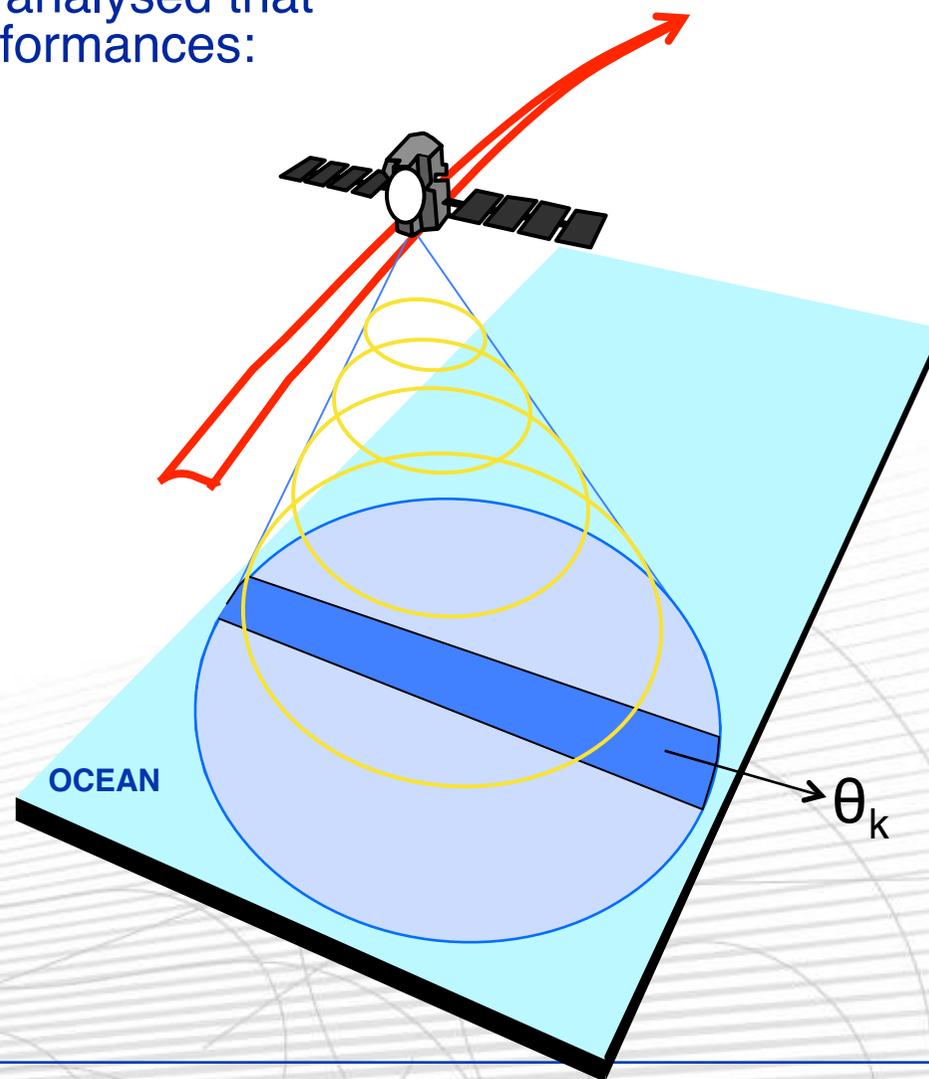


- New L1b processing methodologies are currently being developed
 - new multi-look methodology [Ray et al., 2014],
 - antenna pattern compensation [Scagliola et al., 2014; Dinardo et al., 2015], stack beam weighting)aiming at giving equal weight to all waveforms in the stack
- We propose a new solution: **individual Doppler beams retracker** to optimise the speckle reduction with no beams weighting
- **Alternative SAR processing method to be tested, implemented and assessed**

INDIVIDUAL DOPPLER BEAMS RETRACKER

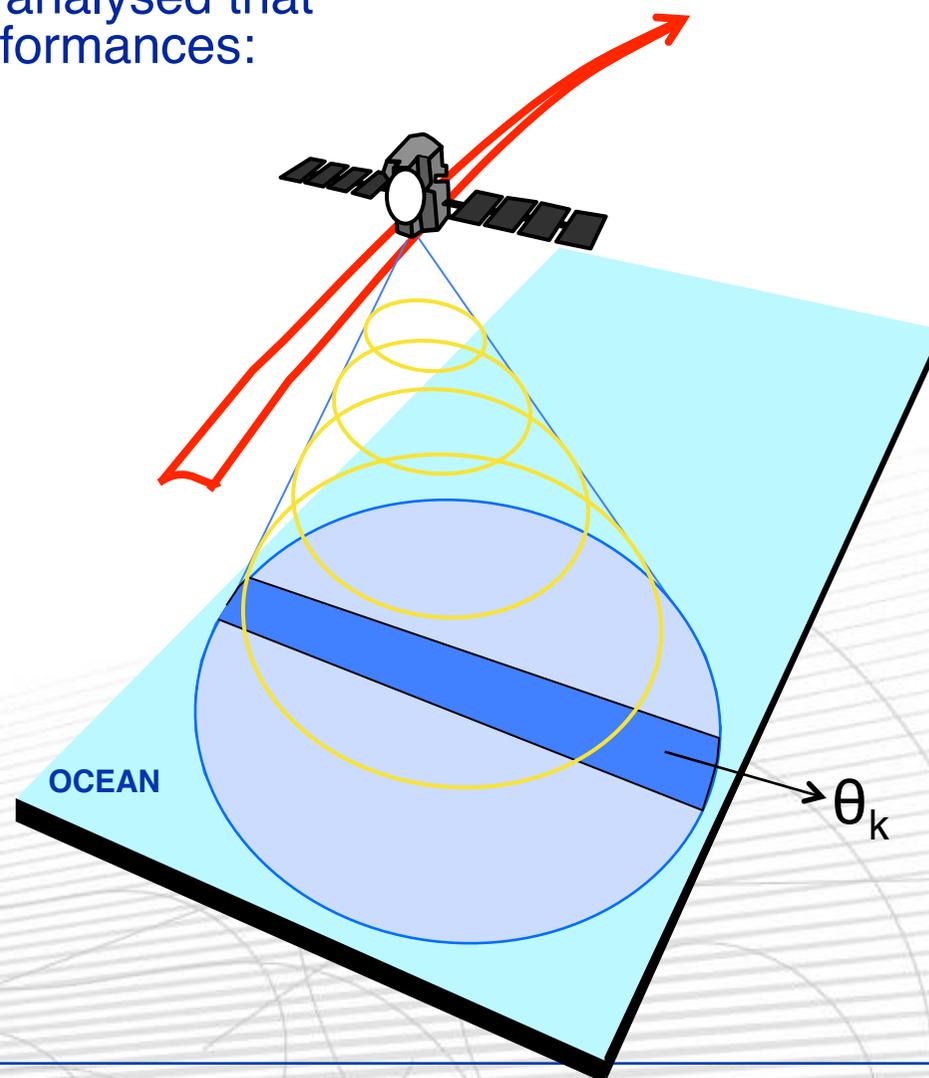
Moreau et al., OSTST, 2015

- An alternative processing method will be analysed that is expected to further improve SARM performances:



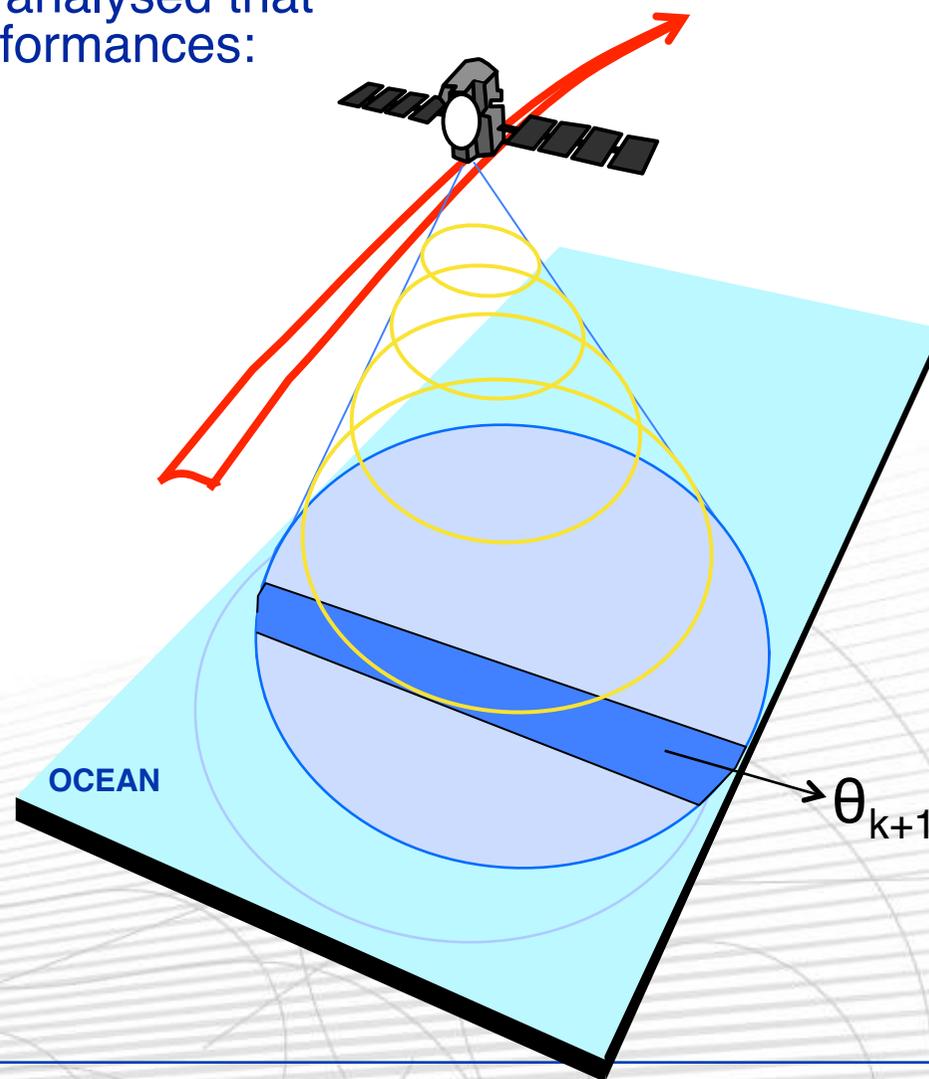
INDIVIDUAL DOPPLER BEAMS RETRACKER

- An alternative processing method will be analysed that is expected to further improve SARM performances:
 - To process each individual look



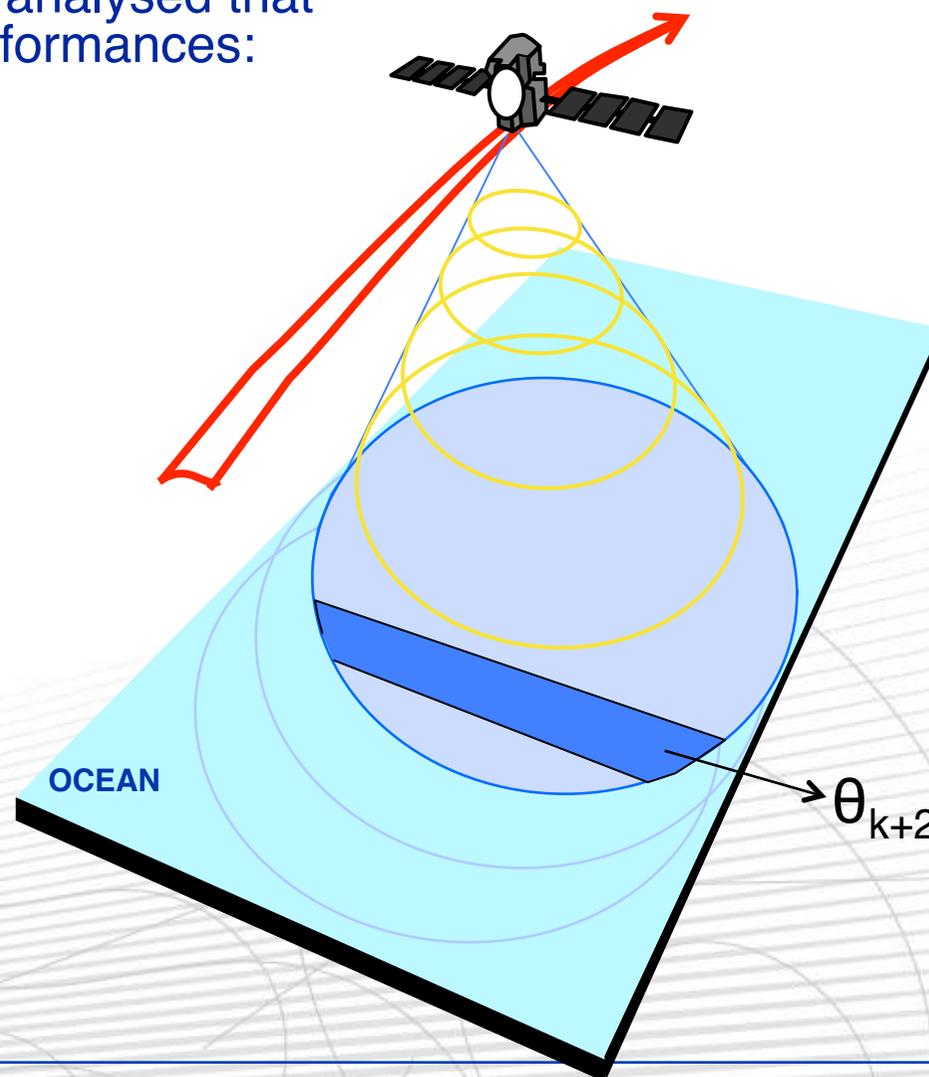
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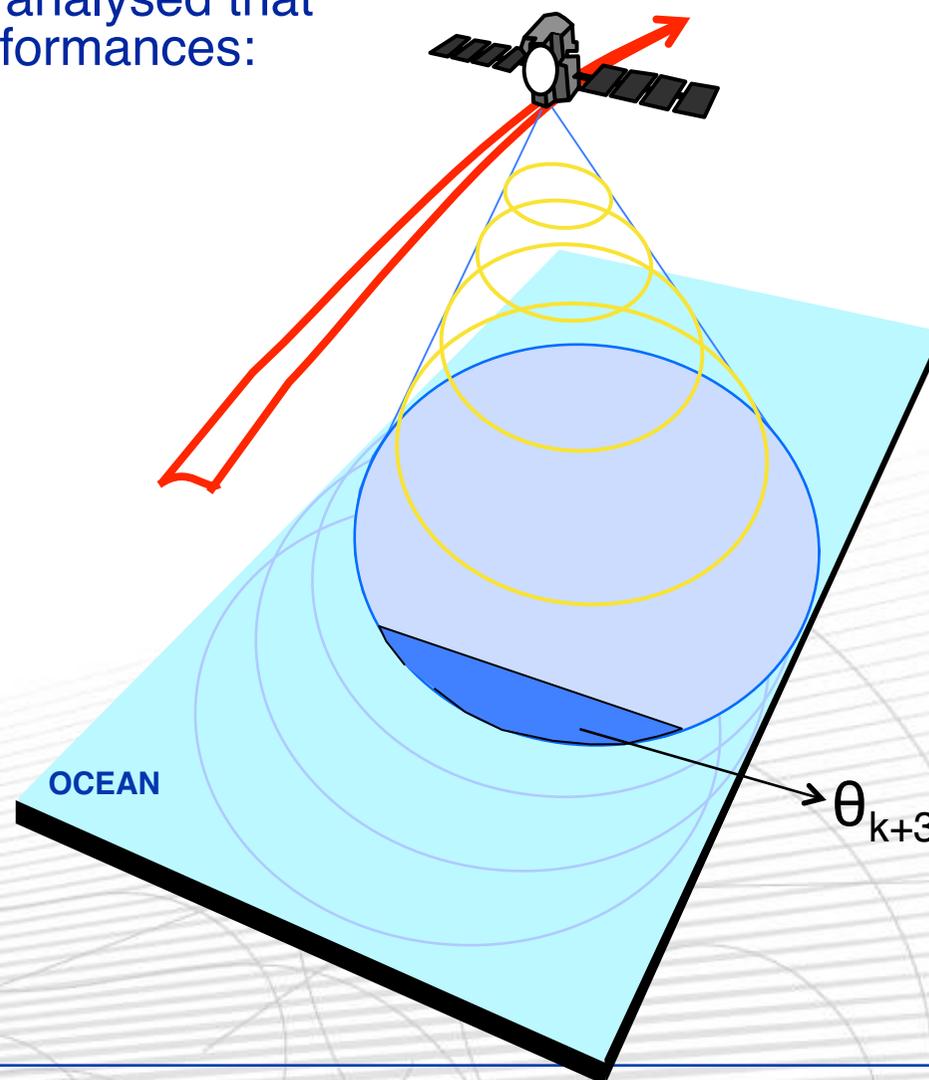
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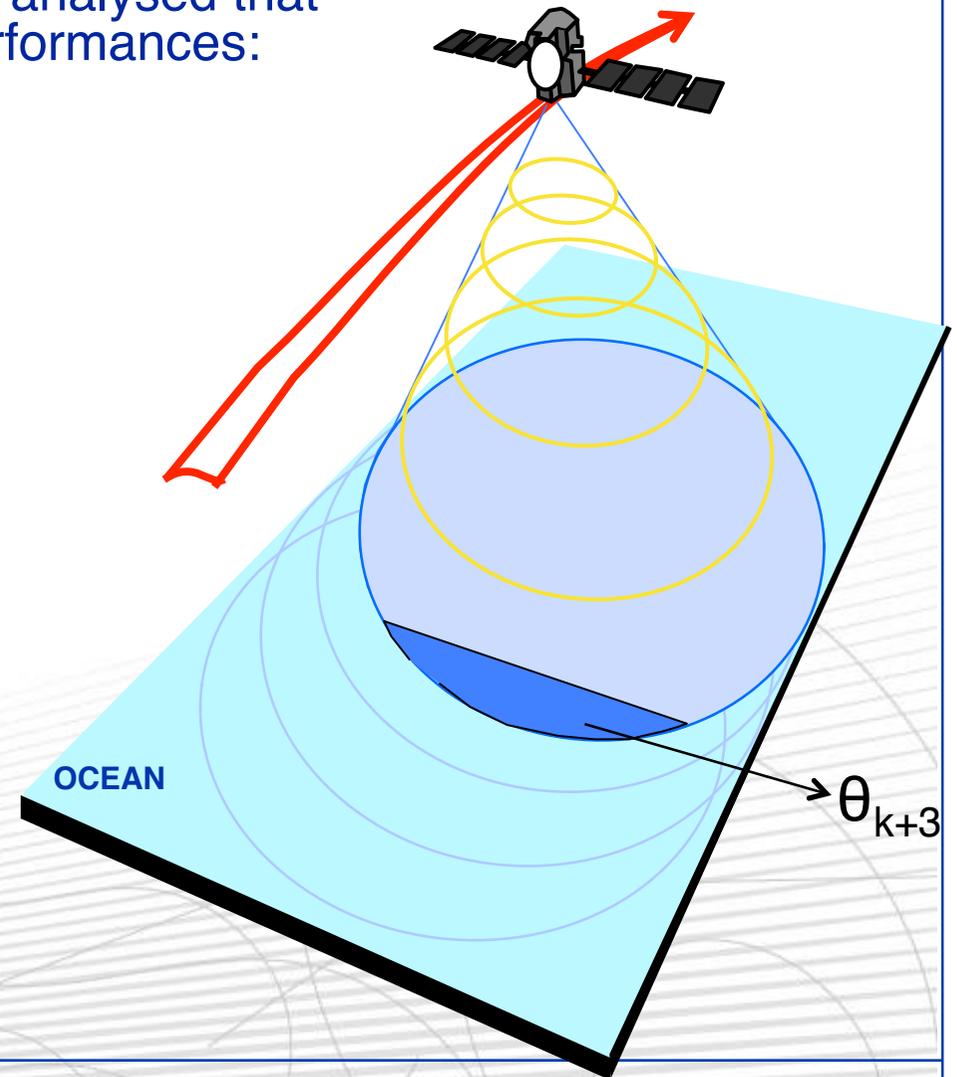
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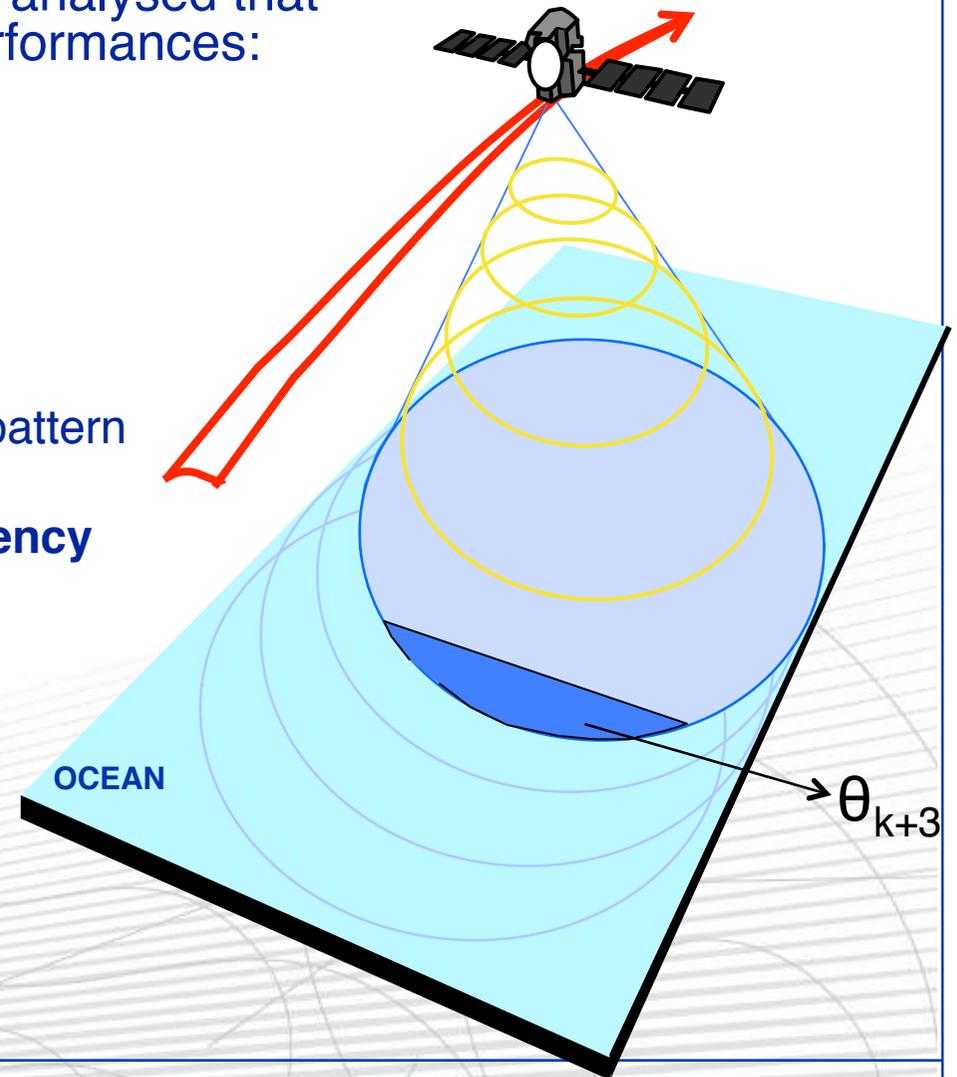
- An alternative processing method will be analysed that is expected to further improve SARM performances:
 - To process each individual look
 - Then “average” their estimates θ_k
$$\theta = 1/L \sum(\dots + \theta_k + \theta_{k+1} + \theta_{k+2} + \theta_{k+3})$$



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$$\theta = 1/L \sum(.. +\theta_k+\theta_{k+1}+\theta_{k+2}+\theta_{k+3})$$
 - ➔ **Making all Doppler beams with equal contribution to the noise reduction**
 - With no beams weighting (e.g., antenna pattern compensation, stack beam weighting)
 - ➔ **Enabling to assess the model consistency (checking any discrepancies between nadir/off-nadir look estimates)**



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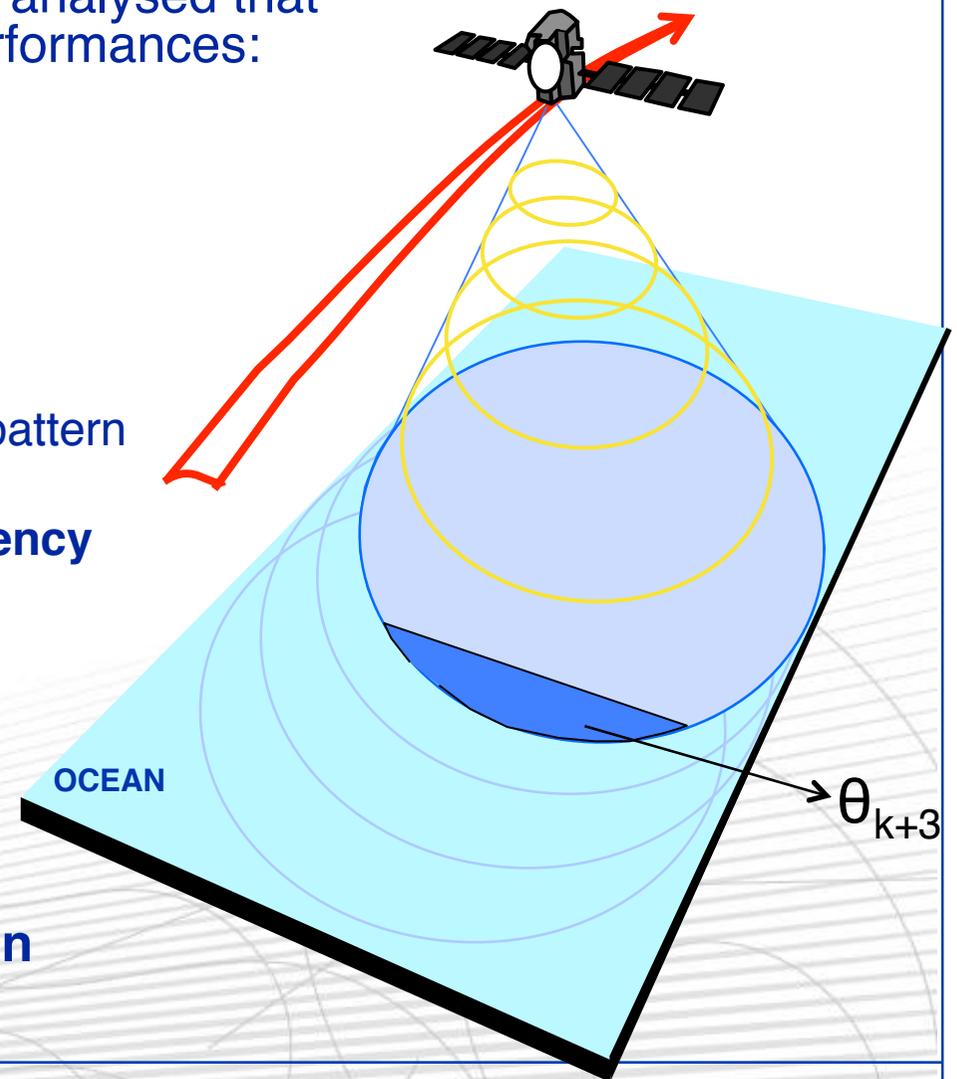
→ **Making all Doppler beams with equal contribution to the noise reduction**

- With no beams weighting (e.g., antenna pattern compensation, stack beam weighting)

→ **Enabling to assess the model consistency (checking any discrepancies between nadir/off-nadir look estimates)**

- Beams alignment before multilooking can be disrupted by inaccurate COR2 command (computed on-board)

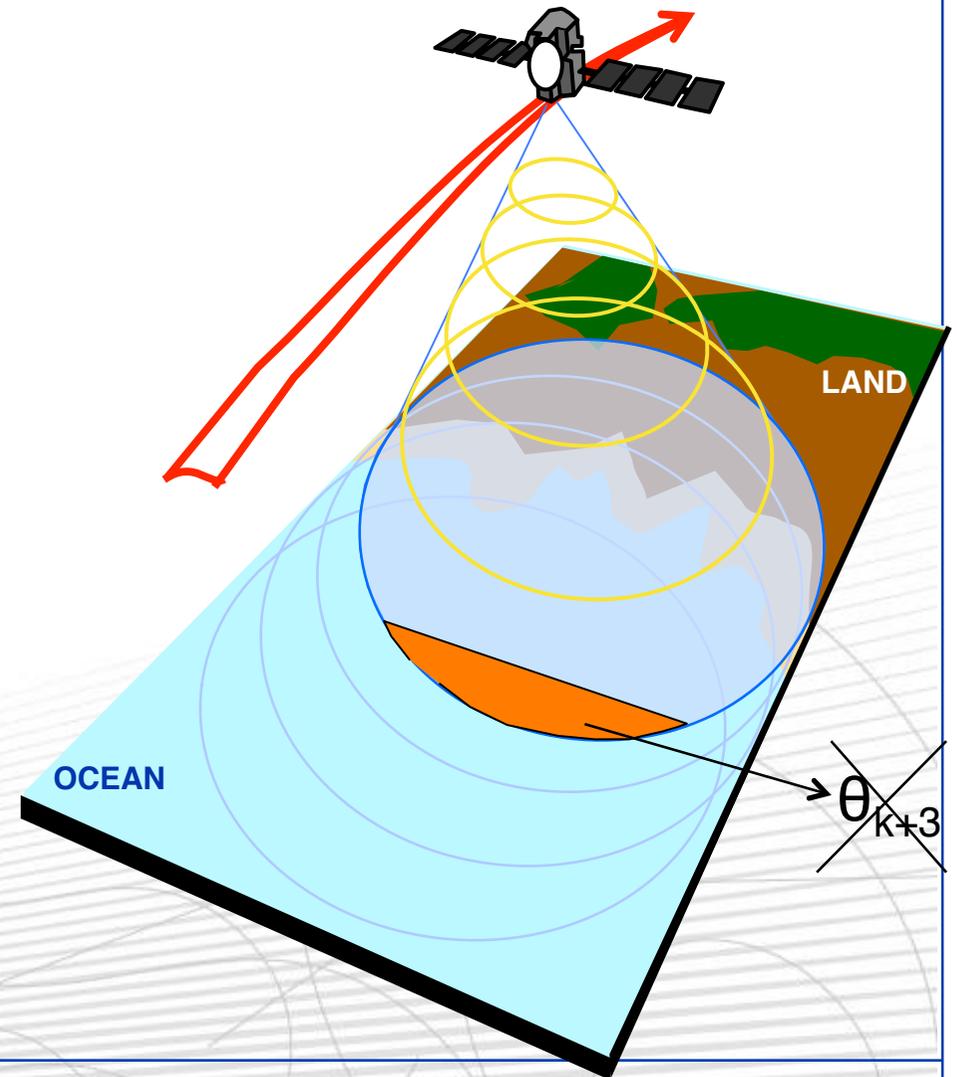
→ **Tracker range alignment is not applied herein (only distance migration correction) mitigating possible errors**



INDIVIDUAL DOPPLER BEAMS RETRACKER

- No valuable data for tracks perpendicular to the coast line at distance < 2-3km despite its high along-track resolution
 → To edit inconsistent looks still contaminated by land / calm sea (or disrupted by possible on-board tracking error)

$$\theta = 1/L \Sigma(.. +\theta_k + \theta_{k+1} + \theta_{k+2} + \cancel{\theta_{k+3}})$$



INDIVIDUAL DOPPLER BEAMS RETRACKER

- **Speckle x is a multiplicative noise of exponential distribution**

Power return echo $y_t = S_t x$ (with S_t the model)

- The density of an exponential law:

$$f(x) = e^{-x} \mathbf{I}_{\mathbb{R}^+}, \text{ giving } f(y_t) = e^{-\frac{y_t}{S_t}} \frac{1}{S_t} \mathbf{I}_{\mathbb{R}^+}$$

- The log-likelihood function estimator algorithm

$$\text{Ln}(f(y_1, \dots, y_k)) = \text{Ln}\left(\prod_{t=1}^k f(y_t)\right) = \text{Cste} - N \sum_{t=1}^k \frac{y_t}{S_t} - \sum_{t=1}^k \text{Ln}(S_t)$$

- To find the maximum of the log-likelihood, we calculate the derivatives of the log wrt parameters and set it to zero

$$\frac{\partial \text{Ln}(f(y_1, \dots, y_k))}{\partial \theta_m} = 0 \quad \rightarrow \quad \sum_{t=1}^k \frac{\partial S_t}{\partial \theta_m} \left[\frac{y_t - S_t}{S_t^2} \right] = 0$$

- **Same criteria as found for the conventional Newton-Raphson algorithm (MLE)** and for Levenberg-Marquardt method (TBC) to solve the system and infer geophysical parameters

→ No change foreseen in the iterative estimation method even if the likelihood function is different (any bias?)

Task

- Test to be done with CPP data and the associated SAR model
 - Adapt and tune the retracking algorithm based on the SAMOSA model (v2.5 ?) to retrack individual looks done in WP4000
 - Implement modifications to the S-3 processing scheme, and generate L1B test data sets phase 2 of the open ocean and coastal zone.
- ➔ **The new method(s) shall allow a better processing to take maximum advantage from the Doppler processing (improving the SARM capabilities)**

Deliverables

- Product Specification Document D2.3
- Source Code of Prototyped Algorithms (initial and updated) D2.10
- Software/Problem Management Tool D2.11
- Updated POCCD
- Updated ATBD(s) D1.3
- L1B Test Data Set for Phase 2

Risks (N/A)

Recommendations

- Close collaboration with WP4000 team for the development of the associated retracker (L1B to L2) processing

- Amarouche L., SAR altimetry: a comprehensive approach from theoretical studies to instrument processing and geophysical validation, SAR Altimetry Expert Group Meeting, NOC, Southampton, UK, 26-27 june 2013
- Ray C., Roca M., Martin-Puig C., Garcia A., Escola R., A new multi-look methodology for SAR altimetry, OSTST, Lake Constance, 2014
- Scagliola M., Fornari M., Tagliani N., Di Giacinto A., Speckle reduction on SAR waveforms by along-track antenna pattern compensation on stacks of single look echoes, OSTST, Lake Constance, 2014
- Dinardo S., Scagliola M., Fornari M., Benveniste J., Level-2 assessment of along-track antenna pattern compensation for SAR altimetry, OSTST, Reston, 2015
- Moreau T., Amarouche L., Aublanc J., Vernier A., Thibaut P., Boy F., Picot N., Improved SAR-mode ocean retrievals from new Cryosat-2 processing scheme, OSTST, Reston, 2015