## D4.1 Algorithm Theoretical Baseline Document - SAR Mode Coastal and Open Ocean Data Products produced by ESRIN

## 1. INTRODUCTION

This document describes the algorithms used by Salvatore Dinardo and Bruno Lucas (both of ESRIN) to generate a set of CryoSat-2 SAR Data Products for Application over the Coastal and Open Ocean, using the SAMOSA echo model. This document has been compiled by David Cotton (SatOC) based on information from SD and BL.

## 2. OVERVIEW

Table 1 lists the set of CryoSat-2 SAR data products that were generated by ESRIN (and NOC) using the SAMOSA echo model for open and coastal ocean applications:

| Run <br> Reference | C2 L1B <br> Product | L2 SAR <br> retracker <br> model | A/pha-p <br> LUT | Peel <br> Effect <br> applied | Motivation |
| :--- | :--- | :--- | :--- | :--- | :--- |
| ESRIN R1 | CPP | ESRIN SAM2 | Yes | Yes | Full SAMOSA analytical <br> model (Guassian waves <br> statistics |
| NOC R2 | CPP | NOC SAM3 | No | No | Consistent with Sentinel 3 <br> DPM except for treatmen <br> of Thermal Noise. Only <br> small data set available <br> for benchmarking |
| ESRIN R3 | CPP | ESRIN SAM3 | Yes | Yes | To quantify impact on <br> retrieval of omitting f1 <br> term in SAMOSA3 |
| ESRIN R4 | CPP | ESRIN SAM3 | Yes | No | Consistent with Sentinel 3 <br> DPM but with inclusion of <br> alpha_p LUT |
| ESRIN R5 | ESRIN | ESRIN SAM2 | Yes | Yes | Possible impact of L0 - > <br> L1B processing |
| ESR | ESRIN SAM3 | No | No | Consistent with Sentinel 3 <br> DPM baseline |  |

Table 1: Summary of SAR L2 Data sets produced using the SAMOSA echo model.
All except the NOC R2 data products are generated for the Pacific and NE Atlantic SAR regions, and for the months July 2012 and January 2013. The S3 DPM is described in Reference 1.

The data product analysed in the Impact Assessment (WP5000) is ESRIN R1. All of the data sets in Table 1 are assessed in the Coastal Ocean Product Validation report produced by NOC.

## 3. ALGORITHM DESCRIPTION

The general processing approach for SAR (Delay Doppler) L1b is described in Reference 2.
This document deals with the generation of Level 2 data from Level 1b. The following standards were applied:

- The Reference Time for the TAI Datation is 01/01/2000 00:00:00
- The Vertical Datum for altitude reference is the Topex/Poseidon Ellipsoid
- The SAR Return Power Model is SAMOSA (reference 3)
- If the SAMOSA2 model is se with Gaussian PTR approximation corrected by the usage of Look-up Table
- The Curve Best-Fitting Scheme is a Bounded Levenberg-Marquardt LeastSquares Estimation Algorithm (LEVMAR-LSE)
- No Static bias has been applied to the range, wave height and sigma nought measurements / Static bias has been applied to the range, wave height and sigma nought measurements - the values of the static biases are reported in the output NetCDF data products
- The Doppler Shift Correction has been applied to the range measurements
- The internal path delay has been not applied to the range measurements
- The orbital altitude has not been corrected for the Time Tag Bias / The orbital altitude has been corrected for a Time Tag Bias. The value of the applied time tag bias is reported in the output NetCDF data products.
- The measurements are posted either 20 Hz and 1 Hz rate
- Geo-corrections (not available in input CPP L1b products) and sea state bias correction have not been applied.
- No a priori editing has been applied to the 20 Hz measurements
- The misfit between SAR Waveform Model and SAR Waveform Data has been computed as:
sqrt( 1/128*(residuals).^2 )*100
where residuals are the differences between model's waveform power and data's waveform power, normalised for the waveform power's maximum value
The residuals have been computed ruling out from the data's and model's waveform return power the first 12 and last 12 range bins (CPP standard).

Table 2 (from Reference 4) lists the L2 processing options applied with the SAMOSA echo model:

| SAMOSA Retracking Scheme (L2) Processing Options |  |
| :--- | :--- |
| RIR used to compute the Doppler model | Gaussian Function, $\boldsymbol{\alpha}_{\mathrm{p}}$ dynamically extracted at real <br> time from LUT |
| AIR used to compute the Doppler model | Gaussian Function, $\boldsymbol{a}_{\mathrm{p}}$ dynamically extracted at real <br> time from LUT |
| Peeling of the Delay Doppler Map (DDM) | APPLIED |
| Thermal Noise Handling | In input to the re-tracking scheme and measured from SAR <br> Echo's early samples |
| Mis-pointing Handling | Mis-pointing angles in input to the retracking scheme and <br> read from CPP products |
| Multi-looking Handling | Multi-looked Echo Model built accumulating the same <br> number of looks as accumulated at L1b stage to build the <br> data waveform |
| Waveform Normalization | Applied with a moving window size of 1 range bin (i.e. <br> normalization by waveform absolute maximum) |
| Input Waveform Sub-setting | NOT APPLIED |
| SAMOSA Model Generation | SAM3 or SAM2 |
| Skewness Effect | NOT APPLIED |
| Scattering Amplitude Decay Rate (nu) | set to zero |
| Slope (Orbital and Surface) Effect | NOT APPLIED |
| Re-tracking Algorithm | Bounded Levenberg-Marquardt Least Square Estimator <br> $($ LEVMAR-LSE) |

Table 2: SAMOSA L2 Processing Options

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is true?

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Below are provided further details on how to:

- build and apply the $\alpha_{p}$ look-up table (LUT) for the SAMOSA 3 Model
- "peel-off" the SAMOSA-3 Delay Doppler Map


### 3.1 Building $\alpha_{p}$ Look Up Table: Methodology and Application

The $\alpha_{p}$ LUT is built and applied following the steps listed below:

- for each SWH value in input (SWH ranging between 0.1 meter and 10 meter) and for a fixed epoch value (zero), the numerical SAMOSA model and the analytical SAMOSA 3 model are generated using exactly the same radar parameter and geometrical configuration
- the $\alpha_{p}$ table is built finding, for each SWH in input, the $\alpha_{p}$ value providing the best fit, in rms error term, between the SAMOSA numerical model and the SAMOSA 3 analytical model.
- The $\alpha_{p}$ LUT is applied in real time, (i.e. during the re-tracking algorithm execution), extracting, from the table, the $\alpha_{p}$ value corresponding to the SWH value under iteration.

The calculated $\alpha_{p}$ LUT values are provided in Annex A.


Figure 1: Look Up Table for alpha p

### 3.2 Application of the Delay Doppler Map Peel-Off

The SAMOSA model assumes the existence (on board of CryoSat-2) of a radar tracker with an unlimited (or very long) size for the receiving window. This is not the case for a typical realization of a space-born radar altimeter. The consequence of a limited size of the tracker
window is that, during the slant range correction stage, the Data Stack samples are padded with zeroes and these zero-samples are summed up along with signal samples (not-zeroes) during the L1b multi-looking operation. In order to cope with this operating procedure carried out along the CryoSat-2 L1b Chain, a SAMOSA-3 DDM peeling operation has been proposed before to apply the multi-looking at L2.
The zeroes are placed in the SAMOSA-3 Delay Doppler Map following the methodology described below:

- The delay range of each range gate k in a generic Delay Doppler Map column I (i.e. Delay-Doppler beam) is calculated as:

$$
\delta r_{\mathrm{k}}=\frac{\mathrm{c}_{\mathrm{o}}}{2 \cdot \mathrm{~B}_{\mathrm{r}}}\left[\mathrm{~N}_{\mathrm{s}}-1,-1, \mathrm{o}\right] \quad \text { with } \mathrm{k}=1, . ., 128
$$

- The slant range shift of each beam in the Delay Doppler Map is calculated as:

$$
\delta \mathrm{R}_{\mathrm{l}}=\mathrm{H} \cdot\left(\sqrt{1+\alpha_{\mathrm{E}} \cdot\left(\frac{\mathrm{~L}_{\mathrm{x}} \cdot(\mathrm{l})}{\mathrm{H}}\right)^{2}}-1\right) \quad \text { with } 1=-32, \ldots, 31
$$

- For each DDM column I, zeroes are placed in range gates ( $k, I$ ) for which holds the relation:

$$
\delta r_{k} \leq \delta R_{1} \quad \text { with } k=1, . ., 128
$$

with the notation:
$\left.\begin{array}{|c|c|}\hline \mathbf{c}_{\mathbf{0}} & \text { vacuum speed light } \\ \hline \mathbf{B}_{\mathbf{r}} & \text { Received Bandwidth } \\ \hline \mathbf{N}_{\mathbf{s}} & \begin{array}{c}\text { Number of Range gates } \\ (128)\end{array} \\ \hline \mathbf{H} & \text { Orbital Altitude } \\ \hline \mathbf{L}_{\mathbf{x}} & \text { Along Track Resolution } \\ \hline \mathbf{\alpha}_{\mathbf{E}} & \begin{array}{c}\text { Earth Sphericity Factor } \\ \hline \mathbf{I} \\ \hline \mathbf{k} \\ \hline\end{array} \\ \hline \text { Rang Track Beam Index } \\ (1->31)\end{array}\right]$
where $[a, s, b]$ represents an array from $a$ to $b$ with step $s$.
An instance of pseudo-code statements implementing the proposed process can be:
R=Height.*(sqrt(1+(alpha_E.*(Lx.*(I)./Height).^2))-1);
$\mathrm{R}=$ repmat( $\mathrm{R}, \mathrm{Ns},[]$ );
Dr=repmat(c0./(2.*Br)*(Ns-1:-1:0),[],size(1,2)).';
DDM(R>=Dr)=0;

## 4. GLOSSARY

| ATBD | Algorithm Theoretical Baseline Document |
| :---: | :---: |
| CPP | CryoSat Processing Prototype |
| CS2 | CryoSat-2 |
| DDM | Delay Doppler Map |
| DPM | Detailed Processing Model |
| FBR | Full Bit Rate CryoSat-2 SAR mode data ((un-calibrated, geo-located I and $Q$ individual echoes in time domain) |
| LEVMAR-LSE | Levenberg-Marquardt Least-Squares Estimation |
| LUT | Look Up Table |
| NOC | National Oceanography Centre, Southampton UK |
| PTR | Point Target Respose |
| PVR | Product Validation Report |
| SAMOSA | SAR Altimetry Mode Studies and Applications (SAR altimetry project funded under the ESA STSE programme |
| SAM2 | Simplified version of SAM3 to enable more efficient computation. |
| SAM3 | Full analytical model of the SAR altimeter ocean waveform, developed in the SAMOSA project |
| SAR | Synthetic Aperture Radar |
| STSE | Support to Science Element |
| SWH | Significant Wave Height |
| S3 | Sentinel-3 |

## 5. REFERENCES

Reference 1: Detailed Processing Model of the Sentinel-3 SRAL SAR altimeter océan waveform retracker (latest version) - Available on request from Jérôme Benveniste (ESA/ESRIN)
Reference 2 : Guidelines for the SAR (Delay-Doppler) L1b Processing, ESA, 2013, available here
Reference 3: SAR Altimeter Backscattered Waveform Model (SAMOSA Model Paper), IEEETGARSS, in press
Reference 4: Configuration Control Document for CP40ers who retrack CPP Data, ESA, 2014 (available here)

## ANNEX A

$\alpha_{p}$ Look Up Table
The $\alpha_{p}$ values for the proposed LUT are reported in the below table for each SWH value:

| SWH | Alpha p |
| :---: | :---: |
| 0.1 | 0.473 |
| 0.2 | 0.471 |
| 0.3 | 0.469 |
| 0.4 | 0.465 |
| 0.5 | 0.462 |
| 0.6 | 0.459 |
| 0.7 | 0.459 |
| 0.8 | 0.459 |
| 0.9 | 0.459 |
| 1 | 0.459 |
| 1.1 | 0.459 |
| 1.2 | 0.460 |
| 1.3 | 0.461 |
| 1.4 | 0.462 |
| 1.5 | 0.464 |
| 1.6 | 0.465 |
| 1.7 | 0.467 |
| 1.8 | 0.469 |
| 1.9 | 0.471 |
| 2 | 0.473 |
| 2.1 | 0.475 |
| 2.2 | 0.477 |
| 2.3 | 0.480 |
| 2.4 | 0.482 |
| 2.5 | 0.485 |
| 2.6 | 0.487 |
| 2.7 | 0.490 |
| 2.8 | 0.493 |
| 2.9 | 0.496 |
| 3 | 0.499 |
| 3.1 | 0.503 |
| 3.2 | 0.507 |
| 3.3 | 0.509 |
| 3.4 | 0.511 |
| 3.5 | 0.513 |
| 3.6 | 0.515 |
| 3.7 | 0.518 |
| 3.8 | 0.520 |
| 3.9 | 0.523 |
| 4 | 0.525 |
| 4.1 | 0.528 |
| 4.2 | 0.531 |
| 4.3 | 0.533 |
| 4.4 | 0.536 |
| 4.5 | 0.539 |
| 4.6 | 0.542 |
| 4.7 | 0.545 |
| 4.8 | 0.548 |
| 4.9 | 0.552 |


| 5 | 0.555 |
| :---: | :---: |
| 5.1 | 0.558 |
| 5.2 | 0.562 |
| 5.3 | 0.565 |
| 5.4 | 0.569 |
| 5.5 | 0.572 |
| 5.6 | 0.576 |
| 5.7 | 0.579 |
| 5.8 | 0.583 |
| 5.9 | 0.587 |
| 6 | 0.588 |
| 6.1 | 0.587 |
| 6.2 | 0.588 |
| 6.3 | 0.591 |
| 6.4 | 0.594 |
| 6.5 | 0.597 |
| 6.6 | 0.601 |
| 6.7 | 0.604 |
| 6.8 | 0.608 |
| 6.9 | 0.611 |
| 7 | 0.615 |
| 7.1 | 0.618 |
| 7.2 | 0.622 |
| 7.3 | 0.626 |
| 7.4 | 0.630 |
| 7.5 | 0.633 |
| 7.6 | 0.637 |
| 7.7 | 0.641 |
| 7.8 | 0.645 |
| 7.9 | 0.649 |
| 8 | 0.653 |
| 8.1 | 0.657 |
| 8.2 | 0.662 |
| 8.3 | 0.666 |
| 8.4 | 0.670 |
| 8.5 | 0.674 |
| 8.6 | 0.679 |
| 8.7 | 0.683 |
| 8.8 | 0.687 |
| 8.9 | 0.690 |
| 9 | 0.691 |
| 9.1 | 0.692 |
| 9.2 | 0.693 |
| 9.3 | 0.694 |
| 9.4 | 0.695 |
| 9.5 | 0.697 |
| 9.6 | 0.698 |
| 9.7 | 0.699 |
| 9.8 | 0.700 |
| 9.9 | 0.705 |
| 10 | 0.709 |

For values out of the SWH range [0.1 10] meter, it is proposed to use the $\alpha_{p}$ value corresponding to the nearest tabulated SWH value.

